A state-space stock assessment model for American plaice on the Grand Bank of Newfoundland

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Abstract

The current stock assessment model for American plaice (*Hippoglossoides platessoides*) on the Grand Bank of Newfoundland (NAFO Divisions 3LNO) is a virtual population analysis (VPA). This model does not account for the considerable uncertainty about the landings data for this stock. Retrospective patterns have also been noted in the current assessment with overestimation of spawning stock biomass (SSB) and underestimation of fishing mortality (F). Via a thorough model selection process, we develop a state-space stock assessment model (SSM) for this stock that accounts for the uncertainties in the landings data and reduces the retrospective patterns. Our SSM fit the data well, with overall trends in SSB and average F (ages 9–14) similar to those estimated from the current VPA. The retrospective patterns for the SSM were reduced for both SSB and average F which should lead to the provision of better scientific advice for the management of this stock. An important result from our analysis suggests that the current assumption for natural mortality (M) in the stock assessment model may be too low. The lack of recovery of the stock of American plaice on the Grand Bank has often been attributed to overfishing, however fixing M within the model to be lower than is reasonable may be over-estimating the relative impact of F and subsequently over-stating the contribution of fishing mortality to the lack of recovery of the stock.

Keywords: American plaice, Grand Bank of Newfoundland, state-space models, retrospective patterns, landings data uncertainty

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Introduction

American plaice (*Hippoglossoides platessoides*) on the Grand Bank of Newfoundland (NAFO Divisions 3LNO) supported an important commercial fishery historically,

accounting for over ten percent of the Canadian groundfish fishery in the 1950s (DFO, 2011). The population size declined rapidly in the 1980s due mostly to overfishing and, although there has been no directed commercial fishing since 1994, there has since been little improvement in the state of the population (*see e.g.* Wheeland, 2018). The lack of recovery has been attributed to overfishing, which has occurred mainly through bycatch in the yellowtail flounder, skate, redfish, and Greenland halibut fisheries (Shelton and Morgan, 2005). It has also been suggested that an increase in the natural mortality rate due to changing ocean temperatures may also be contributing to the lack of recovery (COSEWIC, 2009).

The current stock assessment model for Grand Bank American plaice is an ADAPT virtual population analysis (see e.g., Lassen and Medley, 2001) that was introduced in the late 1990s. This model is based on catch-at-age data that are derived in part from landings estimates and does not account for the considerable uncertainty about the landings data (Wheeland et al., 2018). Sources of uncertainty include landings recorded as "unspecified flounder" by some countries in the earliest years of available data (see e.g. Pitt, 1972) and an increase in foreign catch outside the 200 mile economic exclusive zone in the mid-80s (e.g. South Korea reporting "nonspecified flounder", Brodie, 1986). More recently, the lack of scientific observer data in the NAFO Regulatory Area has resulted in the need to estimate landings via various methods, including effort ratios and daily catch records (Dwyer et al., 2016). As a result, the landings data may be under-estimated and a stock assessment model that incorporates uncertainty in these data may therefore provide a better assessment.

Another issue that has been noted in the current assessment for American plaice are retrospective patterns, which are consistent directional changes in estimates of stock size as years of data are removed from the assessment model (Mohn, 1999). Retrospective patterns are caused by changes in the accuracy of the data over time and/or spatial and time-varying population processes that are unaccounted for or mis-specified in the model (see e.g. Legault, 2009). Systematic retrospective patterns can lead to poor management advice as important population processes (e.g. biomass and fishing mortality) may be over- or under-estimated and can result in unsustainable or sub-optimal harvesting advice (Szuwalski et al., 2017). To promote sustainable management advice for American plaice on the Grand Bank of Newfoundland, a stock assessment model that reduces or eliminates retrospective patterns is valuable. State-space stock assessment models are ideally suited for this purpose as they can include random errors in the underlying population dynamics model (i.e. for population abundance and fishing mortality rates) thereby accounting for underlying time-varying population processes that contribute to retrospective patterns. Additionally, state-space models allow for errors in the data (see e.g. Nielsen and Berg, 2014; Cadigan, 2015; Albertsen *et al.*, 2016), which is an improvement to the current VPA that treats the catch-at-age data as known with negligible error. In this paper, we present a state-space stock assessment model for American plaice on the Grand Bank of Newfoundland that reduces the retrospective problem and allows for errors in the landings data.

Materials and Methods

There are two components to a state-space stock assessment model: the process model and the observation model. The process model describes how the state of the unobserved fish stock abundance and fishing mortality rates at a given time depend on previous states. The observation model describes how the survey and commercial data depend on the unobserved states (*see e.g.* Aeberhard *et al.*, 2018).

American plaice Process Model

The model runs for the years y = 1960, ..., 2017 and for ages $a = 1, ..., 15^+$, where 15^+ represents the oldest ages grouped together from ages 15 onwards, called the plus group (see Table 1 for model equations). For simplicity, we will refer to model ages $a = 1, ..., A^+$, and years y = 1, ..., Y. The process model describes how the abundance at age *a* in year *y* (*i.e.* $N_{y,a}$) and the fishing mortality, $F_{y,a}$ change over time. The $N_{y,a}$ for all ages and years are treated as random effects, with the cohort abundance model modelled as:

$$\log(N_{y,a}) = \log(N_{y-1,a-1}) - Z_{y-1,a-1} + \gamma_{y,a}$$
$$\log(N_{y,A^{+}}) = \log[N_{y-1,A^{+}-1} \exp^{-Z_{y-1,A^{-}}} + N_{y-1,A^{+}} \exp^{-Z_{y-1,A^{-}}}] + \gamma_{y,a},$$
(1.1)

where $Z_{y,a} = M_{y,a} + F_{y,a}$ is the total mortality rate given by the sum of the natural mortality rate, $M_{y,a}$ (*i.e.* all mortality unrelated to fishing) and $F_{y,a}$. Here, $M_{y,a}$ is assumed to be known and fixed at 0.50 for ages 1–3, 0.30 for age 4 and 0.20 for all ages 5 and above, except during 1989 to 1996, where it is fixed at 0.53 for all ages 5 and above, as recommended by Morgan and Brodie (2001), 0.83 for ages 1–3 and 0.63 for age 4. This formulation for $M_{y,q}$ for ages 5 and greater is identical to the formulation for the most recent stock assessment model for Grand Bank American plaice. Here we also include ages 1-4, which are not currently used in the stock assessment VPA, with values for M at these ages selected through peer consultation. $F_{v,a}$ is set to zero for ages 1-4, as reported catch at these ages is considered negligible. The $\gamma_{v,a}$ are the process errors, assumed to be independent and normally distributed with variance σ_{pe}^2 to be estimated. The numbers at the first age $N_{v,1}$ are modelled as:

$$\log\left(N_{y,I}\right) = \mu_{R_y} + \delta_{R_y},\tag{1.2}$$

where $\mu_{R_y} = \mu_{R_1}$ for y < 1993 and $\mu_{R_y} = \mu_{R_2}$ for $y \ge 1993$, and the two mean recruitment parameters $\mu_{R_1}, \mu_{R_2} \in (-\infty, \infty)$ account for the large differences in recruitment between the two time periods and are fixed effect parameters to be estimated. The deviations from the mean recruitment δ_{R_y} are assumed to follow a normal distribution with AR(1) correlation across years, with the AR parameters σ_R^2 and ϕ_R to be estimated across the entire time series, as we expect recruitment to be more alike in years that are closer together.

We assume that the fishing mortality rates increase with age, *i.e.*,

$$F_{y,a} = F_{y,a-1} + \delta_{F_{y,a}}, \text{ for } a = 7,...,15.$$
 (1.3)

For ages 5 and 6, $F_{y,a} = \mu_{F_{y,a}} + \delta_{F_{y,a}}$, where $\mu_{F_{y,a}}$ is the mean fishing mortality rate, a fixed effect parameter to be estimated. A separate $\mu_{F_{va}}$ is estimated for ages 5 and 6, for two blocks: 1960-1994 and 1995-2017 (i.e. four fixed effect $\mu_{F_{ua}}$ parameters). The age blocking of the $\mu_{F_{ua}}$'s was chosen to reflect overall fishery selectivity patterns, and the year blocks were chosen to account for the closure of the commercial fishery in 1994. The $\delta_{F_{va}}$ are positive deviations from the fishing mortality rate at the previous age and are treated as random effects. The $\delta_{F_{v,a}}$'s are assumed to follow a normal distribution, with the deviations at the first age, $\delta_{F_{u}}$, assumed to have AR(1) correlation across years with parameters $\sigma_{F_e}^2$, ϕ_{F_e} to be estimated. We treat the $\delta_{F_{y,a}}$'s separately for age 5 fish as visual inspection of the catch-at-age data indicated that age 5 fish were not actively targeted in the earliest years of the fishery. The $\delta_{F_{ya}}$'s at ages 6–15⁺ were treated as a correlated AR(1) process, separable across ages and years, with parameters $\sigma_{F6^*}^2, \phi_{F_{36}}, \phi_{F_{36}}$, be estimated. We fit an AR(1) process across ages and years for age $6-15^+$ because fish that are closer in age and time are expected to have $\delta_{F_{i}}$ that are more similar than those that are further apart. The final formulation for the AR(1) parameters were determined via a model fitting process described in the exploratory process below.

Observation model

The observation model includes data from the commercial fishery and scientific research trawl surveys. There are two basic types of fishery information: total landed weight, and the size (length, weight) and age composition of the landings. Both these sources of information are used to derive annual fishery catch numbers-at-age. In the integrated assessment model philosophy, these data sources should enter into the assessment model fitting via separate observation models (*i.e.* one likelihood component for the age composition and one for the landings). We particularly want to focus our model estimation to include uncertainty in landings. Therefore, for pragmatic reasons, we used landings information (1960-2017) and the catch proportions-at-age (ages 5-15+ during 1960–2017) as independent data sources for model estimation. We only use commercial data from 1960 onwards as there was insufficient sampling before 1960. The current assessment model also does not use data prior to 1960. Age-based indices of stock abundance (i.e. numbers) are derived from the Canadian fall and spring research surveys in NAFO Divs. 3LNO (see Dwyer et al., 2014 for details) and the Spanish research survey in the portions of NAFO Divs. 3NO outside of the Canadian Exclusive Economic Zone (EEZ; González-Troncoso et al., 2017) were also used in model estimation. Indices were for ages 1-15+ for all surveys, for years 1990-2017for the fall survey (2004 and 2014 omitted due to poor survey coverage), 1985–2016 for the spring survey (2006 and 2015 omitted due to poor survey coverage) and 1997–2016 for the Spanish survey.

Catch age composition data

We fit the age composition data using the continuation ratio logit (crl) transformation (*see e.g.* Cadigan, 2015; Berg and Kristensen, 2012; Agresti, 2003). A direct observation model for the matrix of observed catch proportions each year is complicated because of the constraints $P_{oa} \ge 0$ and $\sum P_{oa} = 1$. We use the crl which maps P_a for $a = 1, ..., A_{max}$ into $X_a \in (-\infty, \infty)$ for $a = 1, ..., A_{max} - 1$. The unconstrained crls are derived from the multiplicative logistic transformation,

$$X_{a} = \log \left[\frac{P_{a}}{P_{a+1} + \dots + P_{A_{max}}} \right], a = 5, \dots, A_{max} - 1.$$
 (1.4)

where A_{max} is the plus group. Recall that there is no catch data for ages 1–4. The inverse transformation of (1.4) is:

$$P_{a} = \begin{cases} \frac{\exp(X_{a})}{\prod_{i=1}^{s}(1+\exp(X_{i}))}, & a = 5, ..., A_{max} - 1\\ \frac{1}{\prod_{i=1}^{d}^{-1}(1+\exp(X_{i}))}, & a = A_{max}. \end{cases}$$
(1.5)

The crls for the observed catch proportions-at-age data (*i.e.* $X_{oy,a}$) are calculated from (1.4) and the observation model we use is based on assuming the model residuals $(X_{oy,a} - X_{y,a})$ have a normal distribution with AR(1) correlation separable across ages and years with parameters $\phi_{C_{a}}, \phi_{C_{y}}, \sigma_{C_{y,a}}^2$ to be estimated, as we expect the crl errors to be similar for fish that are closer in age and time. Various age and year formulations were explored for $\sigma_{C_{y,a}}^2$ and are described in the exploratory process below.

Process model		
Recruitment	$\log(N_{\rm ext}) = \mu + \delta$	$\boldsymbol{\delta}_{R_{y}} \sim N(\boldsymbol{\mu}_{R_{y}}, \boldsymbol{\sigma}_{R})$
	$-\sigma(-y, p) = r_{R_y} - r_y$	AR1(y) in δ_{R_y}
		$\mu_{R_1} \text{ for } y \leq 1993 \ \mu_{R_2} \text{ for } y > 1993$
Abundance	$\log (N_{y,a}) = \log (N_{y^{-1,a^{-1}}}) - Z_{y^{-1,a^{-1}}} + \gamma_{y,a}$	
	$\log (N_{y,A^{+}}) = \log \left[N_{y^{-1,A^{+}-1}} exp^{-Z_{y^{-1,A^{+}}}} + N_{y^{-1,A^{+}}} exp^{-Z_{y^{-1,A^{+}}}} \right] + \gamma_{y,a}$	$\gamma_{y,a} \sim N(0,\sigma_{pc})$
Fishing mortality		$\delta_{F_{y,a}} \sim N(0,\sigma_{F_5};\sigma_{F_6})$
2	$F_{y,a} = \mu_{F_{y,a}} + \delta_{F_{y,a}}$ for $a = 5.6$	AR1(y) in $\delta_{F_{y,s}}$
	$F_{y,a} = F_{y,a-1} + \delta_{F_{y,a}}$ for $a = 7 - 15$	AR1(y, a) in positive $\delta_{F_{y,\delta^+}}$
		μ _{Fya} for ages 5, 6, for 1960–1994/1995–2017
Observation model		
Landings	Censored likelihood:	$\epsilon_{L} \sim LN(0,0.05)$
	$\Pr(B_{ly} \leq L_{y} \leq B_{uy}) = \Phi\left\{\frac{\log(B_{uy}/L_{y})}{\sigma_{LC}}\right\} - \Phi\left\{\frac{\log(B_{ly}/L_{y})}{\sigma_{C}L}\right\}$	
Age composition	$\mathbf{X}_{\mathbf{O}_{ay}} = \mathbf{X}_{a,y} + C_{y,a}$	$\epsilon_{c_{y,a}} \sim LN(0,\sigma_{c_{y,a}})$
Survey indices	$I_{s,y,a} = q_{s,a} N_{y,a} \exp^{-f_{s,y}Z_{y,a}} + \epsilon_{I_{s,y,a}}$	$\epsilon_{I_{s,y,a}} \sim N(0, CV_s \cdot I_{s,y,a}),$

 $q_{_{s,a}} = q_{_{s,a-1}} + \delta_{q_{_{s,a}}},$

Table 1. State-space model equations (see corresponding sections for details).

Landings data

Catchability

Dwyer *et al.* (2016) reported uncertainties about the reliability of the landings data for Grand Bank American plaice. To account for this, we treat reported landings as a lower bound for true landings (*i.e.* not all catches are reported). We assume that there is an upper bound for landings that varies with the reliability of data (see Table 2 for details). We used a censored likelihood approach in which the bounds are treated as the only information about landings (*see e.g.* Hammond and Trenkel, 2005; Bousquet *et al.*, 2010; Cadigan, 2015; Van Beveren *et al.*, 2017). We assume the true landings could be accurately estimated with a CV of 5%. Let B_{ly} and B_{uy} denote the lower and upper bounds and $\sigma_L = 0.05$. The negative loglikelihood (nll) for the landings bounds data is:

$$\operatorname{nll}(L_1, \dots, L_Y | \{B_{ly}, B_{uy}; y = 1, \dots, Y\} |) =$$

$$\sum_{y=1}^{Y} \log \left[\Phi \left\{ \frac{\log(R_y/L_y)}{\sigma_t} \right\} - \Phi \left\{ \frac{\log(R_y/L_y)}{\sigma_t} \right\} \right], \quad (1.6)$$

δ_{q_{s,a}} are positive separate q for Campelen and Engel trawls for ages 1–4 for fall and spring

where L_1, \ldots, L_γ are the model predicted landings. We fixed σ_L at a small value to ensure that the estimates of landings are between the bounds for most years.

The Baranov catch equation is used to model commercial catch as a function of N, F and Z,

$$C_{y,a} = \frac{F_{y,a}}{Z_{y,a}} \left(1 - \exp^{-Z_{y,a}} \right) N_{y,a}.$$
 (1.7)

Model predicted catch proportion at age $(P_a = C_a / \sum_a C_a)$ were fit to observed proportions, as described in the previous section. Commercial average weights-at-age $(W_{y,a})$ were calculated by Rivard's method (Rivard, 1980) and are used to calculate model predicted landings each year, $L_y = \sum_a W_{y,a} C_{y,a}$.

Survey data

The model-predicted catch for survey *s* is:

$$I_{s,v,a} = q_{s,a} N_{v,a} \exp^{-f_{s,v} Z_{y,a}}$$
(1.8)

where f represents the fraction of the year the survey takes place (0.460 for the Canadian spring and Spanish surveys and 0.875 for the Canadian fall survey). As in our treatment of the fishing mortality rates, we model the survey catchabilities, $q_{s,a}$, as increasing with age for each survey:

$$q_{s,a} = q_{s,a-1} + \delta_{q_{s,a}},$$
 for a=2,...,15

Here, the $\delta_{q_{s,q}}$ are positive deviations from the $q_{s,q}$ in the previous year and are treated as fixed effects. We note that the δ_q are always positive to ensure that the q's increase with age and are treated as fixed effects since they are part of the observation equation and not the unobserved population process. For age 1 fish, the q_{sa} parameters are freely estimated, with no added deviation. In 1995 the trawl used in the Canadian surveys changed from the Engel to the Campelen (see e.g. Dwyer et. al., 2016). Although Engel catch data were adjusted based on information from comparative fishing to match the Campelen catches, in our model ages 1-4 are given a separate q for each gear period due to issues in conversion of survey catches at these ages (Dwyer et. al., 2016). The indices are assumed to follow a normal distribution, with mean $I_{s,y,a}$ and standard deviation $\sigma_{s,a} = cv_{s,a} \cdot I_{s,y,a}$, where CV_s represents a separate coefficient of variation (CV) parameter for each survey, to be estimated. Various age formulations for each survey CV were explored and are detailed in the exploratory process below. We treated each survey as from an AR(1) process across ages with independent parameters ϕ_s to be estimated. A constant CV variance model for *I* is approximately the same as assuming $\log(I)$ has constant variance; however, an advantage of our approach is that we can use observed zero indices directly in the model whereas in other assessment packages these index zeros are typically excluded which is not appropriate when there are many zeros which occur non-randomly over time.

Estimation

The fixed-effects parameters to estimate (*i.e.* θ) are listed in Table 3. The unobserved states (*i.e.* $\delta_{F_{y,a}}, N_{y,a}$) are integrated out of the joint likelihood function and the estimation of θ is based on maximizing the marginal likelihood $L(\theta)$:

$$L(\theta) = \iiint_{\Psi} f_{\theta}(D|\Psi) g_{\theta}(\Psi) \partial \Psi$$
(1.9)

where Ψ is the vector of all random effects, $f_{\theta}(D|\Psi)$ is the joint probability density function of the data (D; commercial landings, catch proportions at-age, commercial average weights-at-age, and Canadian fall, Canadian spring and Spanish survey indices) and $g_{\theta}(\Psi)$ is the joint probability density function for the random effects. The TMB (Kristensen *et al.*, 2016) package in R is used to integrate the marginal likelihood (1.9), which is performed via the Laplace approximation (*see* Skaug and Fournier, 2006 for details). The nlminb package in R is used to minimize the negative log likelihood function provided by TMB.

Table 2. Upper catch bounds (UB) for estimated landings with associated justification for bounds; RC is reported catch. Discussion on catch uncertainties can be found in Wheeland *et al.* 2018, and references therein

Period	UB	Comments
1960–1976	2xRC	"Unspecified flounder" by some countries. See, for example, (Pitt, 1972).
1977–1982	1.2xRC	Landings by primarily Canada (>95%) after establishment of 200 mile exclusive economic zone (EEZ).
1983–1993	1.5xRC	Increased foreign catch outside 200 miles. Various estimates used for catch estimates. Issues with unspecified flounder records and discarding
1994–2010	1.2xRC	No directed fishing in 1994 (bycatch quota), 0 TAC 1995 onwards. Catches defined from various sources with those considered most reliable by Scientific Council used for totals
2011–2017	1.5xRC	Loss of availability of scientific observer data in the NAFO Regulatory area and surveillance estimates. Varying methods applied to obtain catch estimates including effort ratios (Dwyer <i>et al.</i> , 2016), daily catch records, and NAFO CESAG estimates (NAFO, 2017)

The final model formulation was determined via a thorough exploratory process. The overall goal of the exploratory process was to determine the best model formulation for the survey CVs, the crl σ_c^2 (sds) and the q age-aggregating (detailed below). The Bayesian information criterion (BIC) was used in model selection since BIC penalizes more heavily for extra parameters when the sample size is large. Previous work has shown that the correlation parameters can be difficult to estimate reliably (see, e.g., Johnson et al., 2016; Xu et al., 2019), thus for our exploratory process, we conducted four exploratory runs with fixed AR(1) parameters: S1) ϕ_s freely estimated for each survey, all $\phi_F = 0.90$, $\phi_{C_1} = 0.9$, $\phi_{C_2} = 0.75$; S2) ϕ_s freely estimated for each survey, all $\phi_F = 0.90$, $\phi_C = 0.9$, $\phi_C = 0$; S3) all ϕ_s , ϕ_F , $\phi_C = 0.50$; S4) all ϕ_s , ϕ_F , $\phi_C = 0$. In all cases, the exploratory process began with the simplest model: with one sd parameter estimated for the crls, and one CV parameter per survey (see Table 3) and followed the 6 steps below. Within each step, the model was refit for each assumption (e.g. in step 1 the model was refit 10 times, for q age-aggregating 5,..,14):

- 1) *q* age-aggregating: for each age 5,...,14 fix survey $\delta^+_{q_{sa}} = 0$ for all subsequent ages (*e.g.* $q5^+$ is one run with $\delta^+_{q_{sa}}$ fixed at 0 for ages 6+). *q* ageaggregating selected from run with lowest BIC¹.
- CV combinations: for each survey using q ageaggregating from 1) fit all combinations (pooled and unpooled; see Supplementary Materials 1 for details) of CV ages while keeping one CV parameter for other two surveys. Survey CV formulations for each survey selected from run with lowest BIC.
- *re-check q:* with survey CVs from 2), re-run 1) to check that *q* age-aggregation is the same as in 1)
- 4) *crl sd ages:* with survey CVs from 2) and *q* from 1), fit all combinations of crl sd ages. crl sd age formulation selected from run with lowest BIC.
- 5) *crl sd years:* with *q* from 1), survey CVs from 2), and crl sd ages from 4), fit two scenarios:
 - a. pre/post moratorium split: fit a separate age sd parameter pre/post moratorium for year split start ∈ (1990, 1999)
 - b. moratorium gap: fit one separate sd parameter (no age splitting) for 10-year mortarium gap for year gap start ∈ (1990, 1999).

crl sd year formulation selected from run with lowest BIC from both a and b

6) re-check q: with survey CVs from 2), crl sd ages and years from 4–5, re-do 1) to check that q ageaggregation is the same as in 1)

The best fitting model was selected from step 6 for each of the four runs (i.e. one best fitting model for runs S1-S4 selected via lowest BIC from step 6) and model fit compared across all four via a detailed examination of model residuals and BIC. Evidence of patterns in residuals (i.e. blocks of ages and years having residuals of the same sign, and whether or not overall residual variability matches assumption) was used to evaluate potential model mis-specification. The survey and continuation ratio logit residuals, which are correlated in our observation models, were standardized using the Choleski factorization of their estimated covariance matrix. We did not use the one-step ahead residual method (see e.g. Thygesen et al., 2017) because it does not allow for correlations in the observations. A final model was selected from the four S1-S4 best fitting runs (i.e. via BIC and residual fits) and in the final step, two extra runs were fit; one with all ϕ_{E} parameters freely estimated and all ϕ_{C} fixed and one with all AR(1) parameters freely estimated (O2). These two runs were compared to the run with the fixed AR(1)parameters (O1), and a final model selected from the three. In all subsequent text, SSM will refer to the final model.

The SSM fit was also assessed through retrospective model fitting for the years 2011–2017. Each retrospective model fit used one less year of data (*i.e.* model for year 2011 used data up to 2011) and predicted abundance, biomass, spawning stock biomass and average F's were examined for systematic patterns and the severity of retrospective pattern was assessed using Mohn's rho (*see* Mohn, 1999). Ideally, no discernable directional patterns will be present in the retrospective plots.

Biomass-at-age was calculated by multiplying predicted numbers at age (*i.e.* $N_{y,a}$) and stock weights-at-age, which were estimated externally via a spatiotemporal biphasic Von Bertalanffy growth model (*see* Kumar *et al.*, 2020). Length and age data are collected for American plaice from research survey vessels using a length-stratified age sampling design and Perreault *et al.* (2019) showed that ignoring this sampling design can lead to biased growth model parameter estimates. Kumar *et al.*'s method (2020) accounted for the length-stratified age sampling design. The 3LNO stock weights were combined for each division by weighting the values for each division by the average abundance index at age during 1975–2017. Stock weights prior to 1975 were fixed at the mean values for 1975–77.

¹ Note for *q* exploratory purposes (*i.e.* Step 1), the lowest AIC (Akaike information criterion) was used for model selection, since in all cases, the BIC selected the model with the fewest *q* parameters, and this was considered unrealistic for this stock

Table 3: Base model for exploratory process; a+ is *q* age-aggregation (*e.g.* q5+ is model with *q* deviations fixed at 0 for ages 6+). Age groupings for survey CVs and sd crls are for subsequent ages (*e.g.* a separate sd parameter pooled for ages (1–4) (5–6)(7–15)). *See Supplementary Materials 1* for details.

Туре	Parameters
Bas	e model
Process error variance	σ_{pe}^2
Mean recruitment	μ_{R_1} for $y \le 1993$ and μ_{R_2} for $y > 1993$
Variance and correlation of log-recruitment deviations	$\sigma_{\scriptscriptstyle R}^2, \phi_{\scriptscriptstyle R}$
Mean F	$\mu_{F_{y,x}}$ for ages 5, 6, and two time blocks: 1960–1994/1995–2017
Variance at age 5, 6–15+	$\sigma^2_{\scriptscriptstyle F_5}$, $\sigma^2_{\scriptscriptstyle F6^+}$
Model exp	loration S1-S4
Survey q's	
Canadian spring survey	$\delta_{s,ai}$, for s = Canadian spring, fall, Spanish surveys
Canadian fall survey	s,a'
Spanish survey	a^+ = age aggregation explored for ages 5–14
Survey coefficients of variation	
Canadian spring survey	$cv_{s,a}$, for s = Canadian spring, fall, Spanish surveys
Canadian fall survey	a = various age groupings (1–15)
Spanish survey	
Catch age composition variance	$\sigma_{c_{y_a}}^2$, for a = various age groupings (5–14)
Survey residual correlations	ϕ_s for s=Canadian spring, fall, Spanish surveys
Year-correlation of F deviations at age 5, 6–15+	$\phi_{F_{5}},\phi_{F_{16}},\phi_{F_{76}}$
Catch age correlation	$\phi_{_{C_A}},\phi_{_{C_Y}}$

Estimates of maturity-at-age were taken from Wheeland *et al.* (2018).

Simulation and sensitivity testing

A full simulation study is beyond the scope of this paper; however, we conducted a simple self-simulation test and jittered start on the SSM to examine the reliability of the model estimates (*see e.g.* Cadigan, 2015; Nielsen and Berg, 2014). The self-simulation test randomly generates survey indices and continuation ratio logit catch proportions from the model predictions and assumed distributions detailed above. Process errors and other random effects are treated as fixed when generating the data and the model is re-fitted to the simulated data. This process is repeated 1000 times and estimates of SSB, average fishing mortality rates (ages 9–14), recruitment, variance and autocorrelation parameters are stored. We calculated the relative difference of the estimates for each year (*i.e.* (simulation SSB_y – data-based SSB_y)/ data-based SSB_y) for comparison.

The jittered start test re-fits the model with random noise added to the starting parameter values, generated from N $(0,0.25 \cdot \hat{\mu})$, where $\hat{\mu}$ is the model predicted parameter of interest. The model is re-optimized 100 times and the negative log-likelihood is stored for each iteration. Ideally, we expect an identical model fit from the jittered starting parameter values.

We also examined the model sensitivity to our assumptions about M and catch bounds. A profile likelihood was constructed for a range of $M_{a,y}$'s; that is, $M_{a,y} = M + \Delta M$, where M is the SSM M model formulation and $\Delta M \in$ (-0.1, 0.35). We also re-fit the model with upper catch bounds fixed at half the original model formulation upper bounds (M2) and with the upper catch bounds fixed (M3) at 1% of the reported bounds (*i.e.* "fixed landings"). Model fit for the catch bounds was assessed using BIC and an examination of the retrospective plots.

Results

For brevity, we provide a summary table of the exploratory process that describes the final model from each run (Table 4); additionally, only the full exploratory process results from the best fitting run (S2) are given in Supplementary Materials 1 (SM1) and discussed. For exploratory step 1 (run S2), the model with an age-aggregation of $7+(\delta_{q_{in}}^{+}=0 \text{ for ages } 8+) \text{ had the lowest AIC and this was}$ selected as the age-aggregation for step 2 (see footnote 2 for details and SM1 Table 1). Overall, the BIC for the fall model fits ranged between approximately 9970 and 9890, 9940 and 9860 for the spring survey and 9970 and 9900 for the Spanish survey, indicating the grouping of the Spanish survey coefficient of variations (CVs) provided the least improvement in model fit (SM1 Tables 2-5). This is not surprising since the data for the Spanish survey do not cover the entire 3LNO region and are not as informative as the fall and spring surveys (see, e.g. Wheeland et al., 2018 for more details). Rechecking the q age-aggregation in Step 3 confirmed that the age-aggregation of 7+ provided the lowest AIC and BIC with the new survey CV formulations (SM1 Table 6). The continuation ratio logit (crl) age exploratory runs in Step 4 had BICs that ranged from approximately 9600 to 9570, and the age aggregation of (5-6)(7-11)(12-14) was selected as the final crl sd age formulation (SM1 Table 7). For Steps 5a and 5b, the BICs ranged from approximately 9560 to 9480 (SM1 Table 8). Rechecking the q's in Step 6 confirmed that the age-aggregation of 7+ provided the lowest AIC and BIC with the new survey CV and crl sd formulations (SM1 Table 9). The AIC and BIC from Step 1 with a qage-aggregation of 7+ were 9690 and 9922 in comparison to the Step 6 run that were 9194 and 9481 respectively, indicating a substantial improvement in model fit.

In all four exploratory model scenarios, q7+ was the best formulation for the survey catchabilities (q; Table 4). Overall, the survey CV formulations were similar for all four model formulations. For example, for the fall survey, models S1–S3 provided identical formulations, with S4 (all AR(1) parameters fixed to zero) providing a better fit with an extra CV parameter for ages (2–4). Both the spring and Spanish CV formulations were similar for all four runs, providing the best fit with separate parameters at the oldest and youngest ages. In all formulations, the best fit for the crl sd parameters had a separate variance parameter from 1990–1999, with various formulations for the age groupings. For example, S1 provided the best fit with separate sd parameters for ages 5–7,14, and pooled for ages (8–13), whereas S4 pooled the sd parameters for ages (5–11) and (12–14). Overall, S2 had the lowest BIC, and had the best residual fits for both the surveys and the crls (*see Supplementary Materials 2*), and we selected this model as the best fitting model. For the final exploratory step (*i.e.*, one run with all ϕ_F parameters freely estimated and all ϕ_C fixed and one run with all AR(1) parameters freely estimated), the lowest BIC was for the model with all but the crl AR(1) parameters freely estimated (SSM; Table 5), and this was selected as the final state space model.

The SSM fit the data well with no patterns in the survey or continuation ratio logit residual plots (see Supplementary Materials 3). In 2017, recruitment, abundance and spawning stock biomass (SSB) were estimated near the lowest historical levels (Fig. 1). The model predicted landings were estimated within the upper and lower bounds, with the predicted landings closest to the upper bound in the early 80s, and again in 2010 (Fig. 2) and closest to the lower bound in the early 1990s. At ages 1-4, the catchability pattern (Fig. 3) for the fall and spring surveys was lower for the Engels than the Campelen trawl. The differences were most pronounced for ages three and four, with the catchability estimates for the Campelen trawl almost twice as large as for the Engels trawl. For ages 1-5, the process errors (Fig. 4) were close to zero until the mid-nineties. Overall, there were no noticeable trends in the process errors at the older ages. Mohn's rho for the full retrospective run (Fig. 5) was 0.30 for abundance and -0.19 for recruitment. In comparison to the most recent stock assessment model for Grand Bank American plaice (which we refer to as the VPA), the SSM had a lower Mohn's rho for SSB at 0.43 compared to 0.69 for the VPA (Fig. 6). Mohn's rho for aveF for the SSM was almost half the VPA Mohn's rho, at -0.27 for the SSM and -0.45 for the VPA.

The overall trends in SSB and aveF were similar for the SSM and the VPA (Fig. 7). Noticeable differences included the SSM predictions of historical SSB (*i.e.* years 1960–1972) that were larger (but with high uncertainty) than the historical SSB predictions from the VPA. The VPA model also predicted a higher average fishing mortality rate in the early 1990s, at approximately 1.1, with the SSM prediction at approximately 0.80 for the same period.

The self-simulation study lower 2.5% and upper 97.5% intervals for both SSB and aveF covered zero until the mid-1990s,(Fig. 8), indicating that the simulated samples produced estimates that were similar to the SSM estimates in those years. In the earliest years (1960–1972), the median of relative differences for aveF was mostly

Table 4: Best fitting models from exploratory process. For all models, parentheses represent pooled ages and ,,, represent separate ages (*e.g.* 1,.,3(4–12) is a separate sd parameter for ages 1,2,3, and pooled for ages 4–12). (1990–1999) represents a separate crl sd parameter for the year block. S1 is run with ϕ_s freely estimated for each survey, all $\phi_F = 0.90$, $\phi_{C_A} = 0.9$, $\phi_{C_F} = 0.75$; S2 is run with ϕ_s freely estimated for each survey, all $\phi_F = 0.90$, $\phi_{C_A} = 0.9$, $\phi_{C_F} = 0.50$; S4 all ϕ_s , ϕ_{F^2} , $\phi_C = 0$. AIC is the Akaike information criterion and BIC is the Bayesian information criterion.

	S1	S2	S 3	S4
nll	4548	4540	4878	5545
AIC	9216	9194	9861	11196
BIC	9519	9481	10123	11463
		Optimal model f	ormulation	
q	7+	7+	7+	7+
Fall cv	1(2-11)(12-15)	1(2–11)(12–15)	1(2–11)(12–15)	1,(2-4)(5-12)(13-15)
Spring cv	1,,2(3–7)(8–13)(14–15)	1,,2(3–13)(14–15)	1,,2(3–13)(14–15)	(1-2)(3-10)(11-14)15
Spanish cv	1(2-7)(8-15)	1,(2–7)(8–15)	(1-5)(6-15)	(1-5)(6-15)
Crl sd	5,,7(8–13)(1990–1999)	(5–6)(7–11)(12–14) (1990–1999)	5(6–14) (1990–1999)	(5–11)(12–14) (1990–1999)

positive, with the converse for SSB. After 1990, there was a consistent positive bias in aveF and a negative bias in SSB, except in the final years, where aveF was underestimated and SSB overestimated. The boxplots of parameter estimates (Fig. 9) showed that the largest range were for estimated $\mu_{F_{5, Pre1995}}$. TMB has an option (see Thorson and Kristensen, 2016) to reduce bias in nonlinear random effects models, and we implemented this method in a self-simulation run as a potential fix to the bias in our self-simulation study (see M4; Table 5). The bias across the entire time series for both SSB and aveF was much larger with the bias-correction turned on (see Supplementary Materials 4) than without. The jitteredstart test did not converge for 5% of the simulations, with 100% of the converged models producing negative loglikelihoods that were identical to the original formulation.

The minimum negative log-likelihood from the M profile likelihood plot was 4472, with an associated Δ M of 0.30 (Fig. 10). For this model fit, the average fishing mortality rate in 2017 was estimated at 0.01 with SSB in 2017 at 100.83 hundred thousand tons. Results from the sensitivity tests (Table 5) showed that the SSM had a lower BIC than the runs that halved the catch bounds (M2) and "fixed" the landings (M3). This is expected because more narrow catch bounds restrict the flexibility of the model. Mohn's rho for both M1 and M2 for aveF were slightly larger than the Mohn's rho from the SSM at -0.29 (Fig. 11). Similarly, Mohn's rho for M1 and M2 for SSB were slightly larger than for the SSM at 0.39.

Discussion

Overall, our state-space model (SSM) that accounted for uncertainties in the landings data and allowed for process errors fit the data well, with no obvious patterns in the survey and continuation ratio logit residual plots (*see Supplementary Materials 3*). The retrospective patterns were reduced for spawning stock biomass (SSB) and greatly reduced for average fishing mortality for ages 9–14 (aveF) compared to the most recent stock assessment model (VPA).

The M profile plot provided the best fit when M was increased by 0.30, suggesting that the values we used for M's may be too low. Previous research found evidence that M's during 1989 to 1996 (Morgan and Brodie, 2001) had increased to 0.53 and the current VPA model and our SSM include this increase. However, since the closure of the commercial fishery, estimates of total mortality rates have remained high for some periods (e.g. Fig. 7 for years 2000–2006), and this may suggest that M is higher than 0.20 in recent years. This is supported by preliminary work that suggests that M has increased since the mid-1990s (COSEWIC, 2009; Morgan et al., 2011). The lack of recovery of the stock has largely been attributed to overfishing, however the mis-specification of M not only in the SSM but in historical assessment models could be over-estimating the relative impact of F. Thus, although a thorough study of M is beyond the scope of this paper, research that improves our understanding of M for this species should be of high priority as we may be fixing

Table 5. Model estimates of variance parameters and some population parameters with percent (%) coefficient of variation. (O1 is the final model from exploratory runs (S2) with all $\phi_F = 0.9$, $\phi_{C_A} = 0.9$

	SS	М	()1	0	2	Μ	[2	Μ	[3	Μ	4
nll AIC BIC	45 91 94	24 68 70	45 91 92	540 194 481	45 91 94	21 64 71	45 92 95	57 34 37	47 96 99	81 82 84	45 91 94	24 68 70
	Est	CV	Est	CV	Est	CV	Est	CV	Est	CV	Est	CV
$\sigma_{_{F5}}$	2.25	49	1.52	13	2.29	48	2.01	45	2.13	46	2.25	49
$\sigma_{_{F6^+}}$	2.21	20	1.42	8	2.22	19	2.14	19	2.19	19	2.21	20
$\sigma_{_{ m pe}}$	0.22	6	0.22	6	0.22	6	0.23	6	0.23	6	0.22	6
$\sigma_{_{ m R}}$	0.71	15	0.70	14	0.71	15	0.71	14	0.71	14	0.71	15
$\sigma_{_{C5-6}}$	0.60	10	0.56	10	0.53	11	0.61	10	0.61	9	0.60	10
$\sigma_{_{C7-11}}$	0.33	9	0.29	11	0.28	11	0.33	9	0.33	9	0.33	9
$\sigma_{_{C12-14}}$	0.23	13	0.22	13	0.20	13	0.23	13	0.23	13	0.23	13
$\sigma_{_{C90-99}}$	0.95	9	0.98	9	0.76	12	0.96	9	0.96	9	0.95	9
$cv_{Fall 1}$	0.66	20	0.67	19	0.67	20	0.66	20	0.66	20	0.66	20
cv _{Fall 2-11}	0.31	8	0.31	8	0.31	8	0.31	8	0.31	8	0.31	8
cv _{Fall 12-15}	0.45	10	0.45	10	0.45	10	0.45	10	0.45	10	0.45	10
CV _{Span. 1}	1.55	33	1.56	33	1.56	33	1.54	32	1.54	32	1.55	33
CV _{Span. 2-7}	0.81	12	0.81	12	0.81	12	0.81	12	0.81	12	0.81	12
CV _{Span. 8-15}	0.46	11	0.46	11	0.46	11	0.46	11	0.47	11	0.46	11
CV _{Spr. 1}	1.35	28	1.35	27	1.34	27	1.35	27	1.34	27	1.35	28
CV _{Spr. 2}	0.70	18	0.70	17	0.70	17	0.70	18	0.70	17	0.70	18
CV _{Spr. 3-13}	0.37	11	0.37	11	0.37	11	0.37	11	0.37	11	0.37	11
CV _{Spr. 14-15}	0.48	13	0.49	13	0.48	13	0.47	13	0.47	13	0.48	13
$\varphi_{F_{_{\mathcal{M}^\circ}}}$	0.95	2	-	-	0.95	2	0.95	2	0.95	2	0.95	2
φ_{F5}	0.97	4	-	-	0.97	4	0.95	5	0.96	4	0.97	4
$arphi_{F_{_{Y\!6}\cdot}}$	0.98	1	-	-	0.98	1	0.97	1	0.98	1	0.98	1
$\varphi_{_{ m R}}$	0.32	46	0.32	47	0.33	46	0.31	48	0.31	48	0.32	46
$arphi_{ m Fall}$	0.60	8	0.61	8	0.61	8	0.60	8	0.60	8	0.60	8
$\varphi_{\mathrm{Span.}}$	0.70	6	0.69	6	0.70	6	0.70	6	0.70	6	0.70	6
$\varphi_{_{ m Spr.}}$	0.87	3	0.87	3	0.87	3	0.87	3	0.87	3	0.87	3
$\varphi_{_{C_{_{\!\!A}}}}$	-	-	-	-	0.83	4	-	-	-	-	-	-
F ₂₀₁₇	0.11	20	0.11	19	0.11	19	0.09	20	0.08	18	0.09	28
SSB ₂₀₁₇	10.13	16	9.80	16	9.89	16	9.83	17	9.58	17	11.51	18
F _{VPA}	0.06	-	-	-	-	-	-	-	-	-	-	-
SSB_{VPA}	18.24	-	-	-	-	-	-	-	-	-	-	-



Fig. 1. SSM estimated population abundance, spawning stock biomass (SSB), average fishing mortality rate (ages 9–14) and recruitment



Fig. 2. SSM estimated log catch numbers for ages 5–15+ (solid line), the shaded grey represents the region between the log lower catch bounds and the log upper catch bounds.

M within the model to be lower than is reasonable and subsequently over-stating the contribution of fishing mortality to the lack of recovery of the stock.

Mohn's rho from the SSM retrospective analyses for both aveF and SSB were closer to zero than Mohn's rho from the VPA retrospective analysis, which is a key improvement compared to the current assessment model. Including process error in the population dynamics model helped account for underlying time-varying population processes (*e.g.* M) that were not accounted for in the VPA, thereby reducing retrospective patterns. There is still evidence of slight retrospective patterns, and this may be caused by underlying spatial or time-varying processes that are mis-specified in the observation model since process errors can only account for misspecifications in the process equations.

The estimate for survey catchability q is defined as the value required to scale swept-area abundance to the population abundance (see e.g. Dickson, 1993; Fraser et al., 2007). An estimate of q less than one implies that fewer fish are caught than occupied the area of the trawl, and a value greater than one implies that more fish are caught than occupied the area. Bryan et al. (2014) found evidence of herding behavior in over 90% of observed flatfish in the presence of survey trawls and this herding underestimates the width used in area swept calculations and can result in q estimates that are greater than one. Therefore, larger q estimates are not unrealistic for American plaice; however, the q estimates from the SSM are very large, with the maximum at 6.7. The maximum qestimate from the SSM is however much smaller than the maximum q estimated from the VPA at 13.6^2 (Table 26, Wheeland et al., 2018). Additional research is required to better understand why the stock assessment model estimates are so high.

A difference to note between the SSM and the VPA is that the SSM assumes that the survey indices have a normal distribution with a constant coefficient of variation (CV) whereas the VPA assumes that the log of the survey indices have a lognormal distribution. The lognormal distribution does not allow for zeros in the survey data; however, this assumption may not be appropriate when there are many zeros in the data or when zeros are "true" zeros (*i.e.* no fish available to be caught). The assumption of normality with a constant CV avoids the problem of dropping zeros altogether. However, the normal distribution assumption supports negative indices which are infeasible. A solution to this problem is to use a truncated normal distribution



Fig. 3. Survey catchability patterns for the fall, spring and Spanish surveys with a separate catchability for two gear types (Engel and Campelen) for the spring and fall surveys for ages 1–4. Catchability for ages 7+ is fixed at the value for age 7.

in place of the normal distribution (*e.g.* Albertsen *et al.*, 2016). However, a normal distribution with constant CV is virtually identical to a truncated normal distribution when the CV is small. Consider two random variables (*e.g.* X and Y) that both have mean μ and a constant coefficient of variation, $\tau = \sigma/\mu$. If $X \sim N(\mu, \sigma = \tau \mu)$ and $Y \sim TN(\mu, \sigma = \tau \mu; Y > 0)$ has a truncated normal distribution then their density functions differ by a multiplicative constant that only depends on τ and does not depend on μ . The constant is $\int_0^\infty \varphi(\frac{z-1}{\tau}) dz$ where $\varphi(\cdot)$ is the density function for $Z \sim N(0, 1)$. The constant is close to 1 for $\tau < 0.5$. Hence, for our model, using the truncated normal distribution will only affect estimation through differences in the weighting

² Note that the survey index from the NAFO assessment is in millions and the catch is in thousands; to get the qs on the same scale as the SSM we multiplied the NAFO q estimate by 1000



Fig. 4. SSM estimated process errors for ages 1–14 for years 1960–2016.

of survey indices with different τ 's, especially when $\tau \gg 0.5$. For our SSM we only have large τ 's for the Spanish survey and ages 1–2 for the Canadian surveys, thus in our case there should be little difference in model fit for the truncated normal vs the normal. However, although the approaches are theoretically similar, future research is needed to compare the performance of the three methods.

Fitting the age composition and landings data separately is in line with the integrated model philosophy, but our treatment of stock and catch weights is not. Ideally, each source of data should enter independently into the likelihood equation; however, the stock and catch weights at age data for American plaice are collected in complex length-stratified sampling designs and how to model these likelihoods is difficult and beyond the scope of this paper. In the future, state-space stock assessment models will ideally fit to the raw data (*e.g.*, maturity at age, weights at age) and this will require complex stock assessment models that can account for the spatial nature of the stock assessment data.

The self-simulation study lower 2.5% and upper 97.5% did not cover zero for years 2006–2010 and again in

2013–2015. This bias was also present in models O1 (fixing all crl and F AR(1) parameters) and O2 (freely estimating all AR(1) parameters; see Supplementary Materials 4). In a self-test simulation the model is specified exactly so stock size estimation bias cannot be the result of model misspecification, but rather it must be related to estimation bias and possibly related to nonlinear modelling of random effects. Our selfsimulation run that implemented the TMB bias correction option had larger bias than the SSM self-simulation run without (Supplementary Materials 4), which provides evidence that the bias is related to estimation bias. Also, preliminary research that fit the SSM with an increase in M (both across the entire time series, and another run increasing M only in the later years) did not produce the self-simulation bias in SSB and aveF in these later years (see Supplementary Materials 4). Hence, it seems that the bias is related to the particular settings of the model, and perhaps the magnitude of variance parameter estimates, and this requires additional research to better understand this type of bias.

Although M profile plots are useful in providing a general picture of the role of the M assumption, it is also useful to



Fig. 5. SSM retrospective estimates from 2011–2017 for total abundance, spawning stock biomass (SSB), average fishing mortality rates (ages 9–14) and recruitment for years 1960–2017. Mohn's rho is given in the top right corner.



Fig. 6. Retrospective estimates for spawning stock biomass (SSB) and average fishing mortality rates (ages 9–14) for the SSM and VPA for years 1960–2017. Mohn's rho is given in the top right corner



Fig. 7. SSM (solid line) and VPA (dashed line) estimated spawning stock biomass for years 1960–2017 and average fishing mortality rates (ages 9–14) for years 1960–2017. The shaded grey region represents the SSM model predicted uncertainty.



Fig. 8. Relative difference from the SSM self-simulated sample for spawning stock biomass and average fishing mortality rates (ages 9–14). The solid grey line in the median of the estimates and shaded grey regions represent the lower 2.75% and upper 97.5% bounds.



Fig. 9. Boxplots of self-simulated parameter estimates. The asterix represents the SSM (true) parameter estimate.



Fig. 10. Profile plot (top panel) for various ΔM formulations with corresponding average fishing mortality rate (ages 9–14) (aveF; middle panel) and spawning stock biomass (SSB; bottom panel).

examine which data sources are more informative about M, and Lee *et al.* (2011) suggested that informative length or age composition data is needed to reliably estimate M. Data-specific M profiles are commonly produced by more traditional stock assessment models without random effects and process error (*e.g.* SS3; Methot and Wetzel, 2013) but in a state-space stock assessment model it is not straight-forward how to do this because the integrated log-likelihood cannot be split into a sum of log-likelihoods due to various data sources and other model assumptions. Further development of diagnostics designed to detect M misspecification (*e.g.* Cadigan and Farrell, 2002) also seems useful.

While overall trends in stock trajectory are similar, our new SSM is an improvement to the current stock assessment model that is used to inform the management of American plaice on the Grand Bank of Newfoundland as it allows for errors in the landings data and reduces the retrospective patterns. Additionally, the thoroughness of our model selection process has the potential to increase the confidence in the selected final model and thereby in the assessment output that is being provided to fisheries managers. Our results also suggest that the current values used for natural mortality rates may be too low as our diagnostic model fitting found the best model fit when M was increased by 0.30. This is an important note not only for American plaice, but for all stocks that are managed under the assumption of a fixed M. We suggest that M



Fig. 11. Retrospective plots for sensitivity runs. SSM is the final model formulation, M2 is with upper catch bounds set to half the SSM upper bounds, M3 is model with "fixed" landings. Mohn's rho is given in the top right corner.

profile plots (and/or alternative diagnostics) should be routinely provided to facilitate a better understanding of model behavior for various assumptions about M. This can provide motivation for research into more realistic values of M for future stock assessment models. Overall, this model is a valuable first step in improving our understanding of the stock of American plaice on the Grand Bank of Newfoundland as the flexibility of state-space models are an ideal foundation to build more realistic models.

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PERREAULT et al.: A state-space stock assessment model for American plaice on the Grand Bank of Newfoundland 63

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Supplementary Materials 1

Step 1) Exploratory q runs (*e.g.* q5+ is model run with q deviations fixed at zero for ages 6+). In all cases, one cv parm per survey, crl std fixed at 0.20, AR1 crl age/year fixed at 0.9/0, AR1F fixed at 0.90. np is number of parameters, nll is the negative log-likelihood, AIC is the Akaike information criterion and BIC is the Bayesian information criterion.

		q runs		
q	np	nll	AIC	BIC
5+	40	4817	9713	9915
6+	43	4807	9700	9917
7+	46	4799	9690	9922
8+	49	4799	9696	9943
9+	52	4799	9702	9964
10+	55	4799	9708	9985
11+	58	4798	9713	10005
12+	61	4793	9708	10016
13+	64	4789	9706	10028
14+	67	4780	9695	10032

Step 2) For all runs, m_q's for ages 8+ fixed at zero (*i.e.* q_8+=q_7). For all runs below parentheses represent pooled ages and ,., represent separate ages (*e.g.* 1,.,3(4–12) 13,.,15 is sep. sd parm for ages 1,2,3, 13,14,15 and pooled for ages (4–12)). crl sd fixed at 0.20, AR1 crl age/year fixed at 0.9/0, AR1F fixed at 0.90. np is the number of parameters, nll is the negative log-likelihood, AIC is the Akaike information criterion and BIC is the Bayesian information criterion.

		Fall	cv			Spring cv			Spanish cv	
Model	np	nll	AIC	BIC	nll	AIC	BIC	nll	AIC	BIC
(1–15)	46	4799	9690	9922	4799	9690	9922	4799	9690	9922
1(2–15)	47	4795	9683	9920	4777	9648	9885	4795	9684	9921
1,,2(3–15)	48	4795	9685	9927	4768	9632	9874	4794	9684	9926
1,,3(4–15)	49	4795	9687	9934	4768	9634	9881	4791	9681	9928
1,,4(5–15)	50	4795	9689	9941	4767	9635	9887	4789	9678	9929
1,,5(6–15)	51	4793	9687	9944	4767	9636	9893	4783	9669	9926
1,.,6(7–15)	52	4793	9689	9951	4765	9634	9896	4783	9670	9932
1,,7(8–15)	53	4791	9687	9954	4765	9636	9903	4778	9662	9929
1,,8(9–15)	54	4789	9685	9957	4764	9637	9909	4778	9664	9936
1,,9(10–15)	55	4784	9677	9955	4763	9637	9914	4778	9666	9943
1,,10(11–15)	56	4780	9671	9953	4760	9633	9915	4778	9668	9950
1,,11(12–15)	57	4774	9661	9948	4760	9635	9922	4778	9669	9957
1,,12(13–15)	58	4772	9659	9952	4759	9634	9926	4778	9671	9964
1,,13(14–15)	59	4771	9660	9958	4753	9623	9921	4778	9673	9971
1,,15	60	4771	9662	9964	4753	9625	9928	4775	9670	9972
(1–15)	46	4799	9690	9922	4799	9690	9922	4799	9690	9922
(1–14)15	47	4799	9691	9928	4798	9691	9928	4799	9692	9929
(1–13)12,.,15	48	4797	9689	9931	4793	9682	9924	4797	9689	9931
(1–13)12,.,15	49	4786	9669	9916	4793	9683	9930	4794	9686	9933
(1–13)12,.,15	50	4783	9666	9917	4791	9681	9933	4793	9686	9938
(1–13)12,.,15	51	4783	9667	9924	4791	9683	9940	4790	9683	9940
(1–13)12,.,15	52	4782	9668	9930	4786	9677	9939	4788	9680	9942
(1–13)12,.,15	53	4780	9667	9934	4783	9673	9940	4785	9677	9944
(1–13)12,.,15	54	4780	9667	9939	4781	9669	9941	4781	9669	9941
(1–13)12,.,15	55	4777	9664	9942	4774	9658	9935	4780	9670	9947
(1–13)12,.,15	56	4777	9666	9948	4773	9657	9940	4777	9665	9947
(1–13)12,.,15	57	4775	9664	9951	4772	9659	9946	4776	9667	9954
(1–13)12,.,15	58	4775	9666	9958	4768	9652	9944	4776	9668	9960
(1–13)12,.,15	59	4774	9666	9963	4758	9634	9931	4776	9670	9967
(1–13)12,,15	60	4771	9662	9964	4753	9625	9928	4775	9670	9972

Step 2	Fall exploratory runs. For all runs, $m_{-}q$'s for ages 8+ fixed at zero (<i>i.e.</i> $q_{-}8+=q_{-}7$). For all runs below parentheses represent pooled CV ages and ,, resent estimate CV ages (2, 1, 2,
com a)	TESCHI SCHRISTIC CV ages (e.g. 1), $(7-12)$ 13), $(1-12)$ 13, $(1-12)$ 13, $(1-12)$ 13, $(1-12)$, $(1-12)$
	year fixed at 0.9/0, AR1F fixed at 0.90. np is the number of parameters, nll is the negative log-likelihood, AIC is the Akaike information criterion and E
	is the Bayesian information criterion.

66

		Fall	1				F	all 2				Fall 3		
Model	du	lln	AIC	BIC	Model	du	nll	AIC	BIC	Model	du	nll	AIC	BIC
(1–12)13,.,15	49	4786	9669	9916	1,(2-3)(4-12)(13- 15)	49	4780	9658	9905	1,(2-3)(4-11) (12-15)	49	4778	9654	1066
1,(2–12)13,.,15	50	4779	9658	9910	1,(2-4)(5-12)(13- 15)	49	4779	9657	9904	1,(2-4)(5-11) (12-15)	49	4777	9652	6686
1,,2(3–12) 13,.,15	51	4779	9660	9917	1,(2-5)(6-12)(13- 15)	49	4780	9658	9905	1,(2-5)(6-11) (12-15)	49	4778	9654	9901
1,,3(4–12) 13,.,15	52	4779	9662	9924	1,(2-6)(7-12)(13- 15)	49	4779	9657	9904	1,(2-6)(7-11) (12-15)	49	4776	9650	9897
1,,4(5–12) 13,.,15	53	4779	9663	9930	1,(2-7)(8-12)(13- 15)	49	4780	9658	9905	1,(2-7)(8-11) (12-15)	49	4777	9653	0066
1,,5(6–12) 13,,,15	54	4778	9664	9936	1,(2-8)(9-12)(13- 15)	49	4780	9658	9905	1,(2-8)(9-11) (12-15)	49	4778	9653	0066
1,,6(7–12) 13,.,15	55	4777	9664	9941	1,(2-9)(10-12) (13-15)	49	4780	9657	9904	1,(2-9)(10-11) (12-15)	49	4778	9654	9901
1,,7(8–12) 13,.,15	56	4776	9665	9947	1,(2-10)(11-12) (13-15)	49	4779	9655	9902	1,(2-10)(11) (12-15)	49	4778	9654	9901
1,,8(9–12) 13,.,15	57	4776	9666	9954	1,(2-11)(12)(13- 15)	49	4776	9651	9898	1,(2-11)(12-15)	48	4778	9652	9894
1,,9(10–12) 13,.,15	58	4775	9665	9957	1,(2-12)(13-15)	48	4780	9656	9898					
1,,10(11–12) 13,,,15	59	4773	9665	9962										
1,.,15	49	4786	6996	9916										
		Fall	4											
Model		lln	AIC	BIC										
1,(2-6)(7-8)(9-11)	50	4776	9652	9904										
1,(2-6)(7-9) (10-11)	50	4776	9651	9903										
1,(2-6)(7-10)(11)	50	4776	9651	9903										

J. Northw. Atl. Fish. Sci., Vol. 51, 2020

Step 2 Spring exploratory runs. For all runs, m_q's for ages 8+ fixed at zero (*i.e.* q_8+=q_7). For all runs below parentheses represent pooled ages and ,., represent separate ages (*e.g.* 1,..,3(4–12) 13,..,15 is sep. CV parm for ages 1,2,3, 13,14,15 and pooled for ages (4–12)). crl sd fixed at 0.20, AR1 crl age/year fixed at 0.9/0, AR1F fixed at 0.90. np is the number of parameters, nll is the negative log-likelihood, AIC is the Akaike information criterion and BIC is the Bayesian information criterion.

		Spi	ring 1				Spi	ring 2				Sprin	ig 3	
Model	np	nll	AIC	BIC	Model	np	nll	AIC	BIC	Model	np	nll	AIC	BIC
1,,2(3–15)	48	4768	9632	9874	1,,2(3-4)(5- 13)(14-15)	50	4760	9620	9872	1,,2(3–4) (5–7) (8–13) (14–15)	51	4757	9617	9874
1,,2(3–14)15	49	4767	9633	9880	1,,2(3–5) (6–13) (14–15)	50	4760	9620	9871	1,,2(3–5) (6–7) (8–13) (14–15)	51	4758	9618	9875
1,,2(3– 13)14,,15	50	4760	9620	9872	1,,2(3–6) (7–13) (14–15)	50	4757	9614	9866	1,,2(3–6) (7)(8–13) (14–15)	51	4757	9616	9873
1,,2(3– 12)13,,15	51	4760	9622	9879	1,,2(3–7) (8–13) (14–15)	50	4758	9616	9868					
1,,2(3– 11)12,,15	52	4760	9623	9885	1,,2(3–8) (9–13) (14–15)	50	4759	9618	9870					
1,,2(3– 10)11,,15	53	4759	9624	9891	1,,2(3–9) (10–13) (14–15)	50	4760	9619	9871					
1,,2(3– 9)10,,15	54	4758	9625	9897	1,,2(3–10) (11–13) (14–15)	50	4760	9619	9871					
1,,2(3– 8)9,,15	55	4757	9625	9902	1,,2(3–11) (12–13) (14–15)	50	4760	9620	9872					
1,,2(3– 7)8,,15	56	4756	9624	9906	1,,2(3–12) (13)(14–15)	50	4760	9620	9872					
1,,2(3– 6)7,,15	57	4754	9623	9910	1,,2(3–13) (14–15)	49	4760	9618	9865					
1,,2(3– 5)6_15	58	4754	9624	9917										
1,,2(3-	59	4753	9623	9921										
1,,15	60	4753	9625	9928										
		Spi	ring 4											
Model	np	nll	AIC	BIC										
1,,2(3–7) (8–9)(10–13) (14–15)	51	4758	9618	9875	-									
1,,2(3–7)(8– 10)(11–13) (14–15)	51	4756	9615	9872										
1,,2(3–7)(8– 11)(12–13) (14–15)	51	4758	9618	9875										
1,,2(3–7) (8–12)(13) (14–15)	51	4758	9618	9875										

		Spani	sh 1				Span	iish 2				Spanish 3		
Model	du	lln	AIC	BIC	Model	du	nll	AIC	BIC	Model	du	lln	AIC	BIC
1,(2–15)	47	4795	9684	9921	$\frac{1,(2-5)(6)(7-1)}{15}$	49	4783	9665	9912	$1,(2-5)(6-7) \\ (8)(9-15)$	50	4778	9657	6066
1,(2–14)15	48	4795	9686	9928	1,(2-5)(6-7) (8-15)	49	4779	9655	9902	1,(2-5)(6-7) (8-9)(10-15)	49	4784	9665	9912
1,(2–13)14,.,15	49	4792	9683	9929	$\begin{array}{c} 1, (2-5)(6-8) \\ (9-15) \end{array}$	49	4781	9659	9066	1,(2-5)(6-7) (8-10)(11-15)	49	4782	9662	6066
1,(2-12)13,.,15	50	4790	9680	9932	1,(2-5)(6-9) (10-15)	49	4782	9661	9066	1,(2-3)(6-7) (8-11)(12-15)	50	4779	9657	6066
1,(2–11)12,.,15	51	4789	9681	9938	1,(2-5)(6-10) (11-15)	49	4782	9662	6066	1,(2-3)(6-7) (8-12)(13-15)	50	4779	9657	6066
1,(2-10)11,,15	52	4787	9678	9940	1,(2-5)(6-11) (12-15)	49	4783	9665	9912	1,(2-3)(6-7) (8-13)(14-15)	50	4779	9657	6066
1,(2–9)10,.,15	53	4785	9676	9943	1,(2-5)(6-12) (13-15)	49	4783	9665	9912	1,(2-3)(6-7) (8-14)(15)	50	4777	9654	9066
1,(2–8)9,.,15	54	4782	9673	9945	1,(2-5)(6-13) (14-15)	49	4784	9665	9912					
1,(2-7)8,.,15	55	4778	9666	9943	1,(2-5)(6-14) (15)	49	4783	9665	9911					
1,(2–6)7,.,15	56	4778	9668	9950	1,(2-5)(6-15)	48	4784	9664	9066					
1,(2–5)6,.,15	57	4775	9664	9952										
1,(2-4)5,.,15	58	4775	9996	9958										
1,(2–3)4,.,15	59	4775	9668	9965										
		Spani	sh 4											
Model	du	lln	AIC	BIC										
1,(2-7)(8-15)	48	4782	9659	9901										

Step 3) Check qs with new survey cvs; Fall grouped 1(2-11)(12–15); Spring grouped 1,2,(3–13)(14–15); Spanish grouped 1(2-7)(8-15). In all cases, crl sd fixed at 0.20, AR1 age for all surveys fixed at 0.90. crl sd fixed at 0.20, AR1 crl age/year fixed at 0.9/0, AR1F fixed at 0.90. np is the number of parameters, nll is the negative log-likelihood, AIC is the Akaike information criterion and BIC is the Bayesian information criterion.

		q run	15	
q	np	nll	AIC	BIC
5+	40	4817	9713	9915
6+	43	4807	9700	9917
7+	46	4799	9690	9922
8+	49	4799	9696	9943
9+	52	4799	9702	9964
10+	55	4799	9708	9985
11+	58	4798	9713	10005
12+	61	4793	9708	10016
13+	64	4789	9706	10028
14+	67	4780	9695	10032

		Ċ	PA					112				51.2		
Model	4		AIC	BIC	Model	44	114	AIC	BIC	Model	44		AIC	BIC
(5-14)	54	4611	9331	9603	56(7–14)	56	4592	9295	9577	(5-6)(7-8)	56	4594	9299	9581
5,(6–14)	55	4608	9327	9604	5,.,6(7–13)14	57	4590	9294	9582	(9-14) (5-6)(7-9) (10-14)	56	4593	9298	9580
5,.,6(7–14)	56	4592	9295	9577	5,.,6(7–12)13,.,14	58	4590	9296	9589	(5-6)(7-10) (11-14)	56	4593	9297	9579
5,.,7(8–14)	57	4589	9293	9580	5,.,6(7–11)12,.,14	59	4584	9286	9583	(5-6)(7-11) (12-14)	56	4590	9291	9573
5,8(9–14)	58	4588	9292	9585	5,.,6(7–10)11,.,14	09	4584	9288	9590	5-6)(7-12) (13-14)	56	4593	9299	9581
5,9(10–14)	59	4586	9291	9588	5,.,6(7–9)10,.,14	61	4584	9290	9597	(5-6)(7-13) (14)	56	4592	9296	9578
5,.,10(11–14)	09	4585	9291	9593	5,.,6(7-8)10,.,14	62	4584	9291	9604	(5-6)(7-14)	55	4594	9297	9574
5,.,11(12–14)	61	4582	9286	9593										
5,.,12(13–14)	62	4580	9285	9597										
514	63	4579	9283	9601										
		C	el PD					Crl 2						
(5-13)14	55	4609	9329	9096	5,.,6(7–8)(9–14)	57	4592	9297	9584					
(5-12)13,,14	56	4609	9330	9612	5,.,6(7-9)(10-14)	57	4591	9296	9583					
(5-11)12,,14	57	4607	9327	9615	5,.,6(7-10)(11-14)	57	4591	9295	9582					
(5-10)11, 14	58	4606	9328	9620	5,.,6(7–11)(12–14)	57	4587	9289	9576					
(5-9)10,,14	59	4604	9326	9624	5,.,6(7–12)(13–14)	57	4591	9297	9584					
(5-8)9,.,14	60	4601	9322	9624	5,.,6(7–13)(14)	57	4590	9294	9582					
(5-7)8,,14	61	4591	9304	9611										
(5-6)7,,14	62	4580	9285	9597										
5,.,14	63	4579	9283	9601										

grouped 1(2-7)(8-15). AR1 crl age/year fixed at 0.9/0, AR1F fixed at 0.90. np is number of parameters For all runs below parentheses represent pooled ages Step 4) crl exploratory runs. For all runs, m_q 's for ages 8^+ fixed at zero (*i.e.* $q_8^+=q_7$), Fall grouped 1(2-11)(12-15); Spring grouped 1,2,(3-13)(14-15); Spanish and ... represent separate ages (e.g. 1...3(4–12) 13...15 is sep. CV parm for ages1.2.3.13,14,15 and pooled for ages (4–12)). np is the number of parameters,

70

J. Northw. Atl. Fish. Sci., Vol. 51, 2020

Step 5a/b) crl exploratory runs by year. For all runs, m_q's for ages 8+ fixed at zero (*i.e.* q_8+=q_7), Fall grouped 1(2–11)(12–15); Spring grouped 1,2,(3–7)(8–13)(14–15); Spanish grouped 1(2–7)(8–15). AR1 crl age/year fixed at 0.9/0, AR1 F fixed at 0.90. np is number of parameters. crl ages grouped (5-6)(7-11)(12-14). np is the number of parameters, nll is the negative log-likelihood, AIC is the Akaike information criterion and BIC is the Bayesian information criterion.

		Crl 1 split		
Model	np	nll	AIC	BIC
PA90	59	4572	9262	9559
PA91	59	4573	9264	9561
PA92	59	4573	9264	9561
PA93	59	4571	9260	9557
PA94	59	4573	9264	9561
PA95	59	4583	9285	9582
PA96	59	4579	9276	9573
PA97	59	4568	9253	9550
PA98	59	4568	9255	9552
PA99	59	4568	9253	9550
		Crl 2 block	ζ.	
P90	57	4540	9194	9481
P91	57	4552	9218	9505
P92	57	4556	9227	9514
P93	57	4559	9232	9520
P94	57	4560	9235	9522
P95	57	4565	9243	9531
P96	57	4593	9300	9587
P97	57	4594	9303	9590
P98	57	4587	9288	9575
P99	57	4583	9280	9568

Step 6) Check qs with new crl sds; crl ages are pooled for ages (5–6)(7–11)(12–14), with a sep sd parm pre/post 1993; Fall grouped 1(2–11)(12–15); Spring grouped 1,2,(3–13)(14–15); Spanish grouped 1(2-7)(8–15) AR1 crl age/ year fixed at 0.9/0, AR1F fixed at 0.90. np is the number of parameters, nll is the negative log-likelihood, AIC is the Akaike information criterion and BIC is the Bayesian information criterion.

		q runs					q runs 2	2				q runs	3	
q	np	nll	AIC	BIC	q	np	nll	AIC	BIC	q	np	nll	AIC	BIC
5+	40	4817	9713	9915	5+	47	4753	9599	9836	5+	51	4572	9246	9503
6+	43	4807	9700	9917	6+	50	4736	9571	9823	6+	54	4553	9213	9485
7+	46	4799	9690	9922	7+	53	4718	9543	9810	7+	57	4540	9194	9481
8+	49	4799	9696	9943	8+	56	4718	9548	9831	8+	60	4540	9199	9502
9+	52	4799	9702	9964	9+	59	4718	9554	9851	9+	63	4539	9205	9522
10+	55	4799	9708	9985	10+	62	4718	9560	9872	10+	66	4539	9211	9543
11+	58	4798	9713	10005	11+	65	4718	9565	9893	11+	69	4539	9216	9564
12+	61	4793	9708	10016	12+	68	4715	9567	9909	12+	72	4539	9221	9584
13+	64	4789	9706	10028	13+	71	4713	9567	9925	13+	75	4539	9227	9605
14+	67	4780	9695	10032	14+	74	4707	9562	9935	14+	78	4535	9227	9620

Supplementary Materials 2

SSM Exploratory model fits; best model formulation









Survey index residuals

Survey index bubble plots

S1



S2





S4



76



Crl fits



Crl fits

78

Crl residuals











Crl bubble plot residuals

year

year

Supplementary Materials 3

Final model fit

Model fit

	60	4524	9168	9470	rel	0.000
Model	nparms	nll	AIC	BIC	conv	maxabs

Estimated landings





Estimated population processes

Survey fits

Fall











Spring

86











model –



Fishing mortality rates



Fishing mortality deviations





Process error

92



Parameter estimates



Catchability estimates





Spanish



Spring



m_q estimates

Fall







Spring









Pearson CRL residuals

Four panel crl residuals



Survey residuals

Standardized survey residuals (red = positive, blue= negative)

Fall



) 2015 1985 1990 1995 2000 2005 2010 2015 1985 1990 1995 2000 2005 2010 2015 year

Four panel survey residuals



Supplementary Materials 4



Self-simulation runs







SSM with $M_{a,y} = M + 0.20$





M4 (with TMB bias correction on)